dtcontrol

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CHAPTER

INTRODUCTION

dtControl is a tool for compressing memoryless controllers arising out of automatic controller synthesis of cyberphysical systems (CPS). dtControl takes as input a controller synthesised by various formal verification tools and represents them in the form of decision trees. In the process, the size of the controller is reduced greatly, and at the same time, it becomes more explainable. While in principle, memoryless strategies in any format can be handled by dtControl, currently it supports controllers output by two tools: SCOTS and Uppaal Stratego. Additionally, there is rudimentary support for strategies produced by PRISM Model Checker and a pipeline with the model checker Storm is under works.

Moreover, it also supports a CSV-based format which allows the user to quickly experiment with the techniques provided by dtControl.

We provide a *User Manual*, which gives information necessary to use dtControl and run the various decision tree learning algorithms implemented in it, as described in the paper "dtControl: Decision Tree Learning Algorithms for Controller Representation" appearing at the 23rd ACM International Conference on Hybrid Systems: Computation and Control (HSCC 2020).

An additional *Developer Manual* is made available for those who are interested in interfacing their own controller synthesis tools with dtControl and/or those interested in implementing their own strategy representation algorithms.

1.1 User Manual

This document equips the user with the information necessary to use dtControl and run the various decision tree learning algorithms implemented in it.

1.1.1 Capabilities

https://youtu.be/https://www.youtube.com/watch?v=qS8FQ3pCeE4

dtControl is a tool to represent controllers using decision trees. It uses decision tree learning to achieve this. The 5-minute video above gives a quick introduction to why and how one may benefit from using dtControl.

The decision tree algorithm running inside dtControl is highly configurable. You may choose to represent a determinized controller, allow for more expressible decision predicates or even tune the heuristic used to pick the best predicate. See *Presets and configuration files* for more details.

While dtControl achieves best results with permissive or non-deterministic controllers with determinization enabled, it can also be used with deterministic controllers. However empirical results with such controllers are not as significant as with non-deterministic controllers.

1.1.2 Getting Started

A quick start installation guide is available in the README. In this section, we elaborate a little more on the installation process.

Installation

Getting dtControl from the Python Package Index (PyPI) is the recommended way to install it. Before running the pip install command, we recommend creating a virtual environment so that dependencies of dtControl do not conflict with any other packages already installed on your system. The official Python documentation for creating virtual environments may help you set it up. However, we provide the most essential information here.

Once you have a recent version of Python 3 installed, you may run:

```
$ python3 -m venv dtcontrol-venv
```

to create the virtual environment in a folder called dtcontrol-venv located in your current directory. You can enter the virtual environment by running:

\$ source dtcontrol-venv/bin/activate

Typically, your shell might indicate that the virtual environment is activated by changing the prompt symbol \$ to something like (dtcontrol-venv) \$. You can now proceed with installing dtControl from PyPI using pip:

(dtcontrol-venv) \$ pip install dtcontrol

Note: In case you want to get the development version of dtControl, you could instead run:

(dtcontrol-venv) \$ pip install git+https://gitlab.lrz.de/i7/dtcontrol.git

Once the dtControl package is installed, the command line interface can be accessed using the dtcontrol command. Try running:

(dtcontrol-venv) \$ dtcontrol -h

If your installation has run successfully, you will now see the help page detailing the usage and arguments.:

```
usage: dtcontrol [-h] [-v] [--input INPUT [INPUT ...]] [--output OUTPUT] [--benchmark-

file FILENAME] [--config CONFIGFILE] [--use-preset USE_PRESET [USE_PRESET ...]] [--

rerun]

    [--timeout TIMEOUT]

    {preset,clean} ...

Scroll to the end of the help message for Quick Start.

optional arguments:

    -h, --help show this help message and exit

    -v, --version show program's version number and exit

input/output:

    --input INPUT [INPUT ...], -i INPUT [INPUT ...]

    The input switch takes in one or more space separated file_

-names or a folder name which contains valid controllers (.scs, .dump or .csv)

    --output OUTPUT, -o OUTPUT
```

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```
The output switch takes in a path to a folder where the.
-constructed controller representation would be saved (c and dot)
  --benchmark-file FILENAME, -b FILENAME
                        Saves statistics pertaining the construction of the decision_
-trees and their sizes into a JSON file, and additionally allows to view it via an_
\hookrightarrowHTML file.
run configurations:
  --config CONFIGFILE, -c CONFIGFILE
                        Specify location of a YAML file containing run_
-configurations. Use along with the --use-preset switch. More details in the User
→Manual.
  --use-preset USE_PRESET [USE_PRESET ...], -p USE_PRESET [USE_PRESET ...]
                        Run one or more presets defined in the CONFIGFILE. If the --
-config switch has not been used, then presets are chosen from the system-level.
\rightarrow configuration file.
                        Special parameters for this switch include 'all', 'all-user',
→ 'all-system'. Refer the User Manual for more details.
                        Rerun the experiment for all input-method combinations.
  --rerun, -r
-Overrides the default behaviour of not running benchmarks for combinations which,
→are already present in
                        the benchmark file.
  --timeout TIMEOUT, -t TIMEOUT
                        Sets a timeout for each method. Can be specified in seconds,
→minutes or hours (eg. 300s, 7m or 3h)
other commands:
  {preset,clean}
                       Run 'dtcontrol COMMAND --help' to see command specific help
Examples:
Create a file storing run configurations
    dtcontrol preset --sample > user-config.yml
Display all presets available with dtcontrol
    dtcontrol preset --config user-config.yml --list
Run the 'my-config' preset on the SCOTS model located at 'examples/cartpole.scs'
    dtcontrol --input examples/cartpole.scs --config user-config.yml --use-preset my-
⇔config
```

The Command-line Interface

This section shows how to configure and run dtControl. For this purpose, we assume that you have an examples folder in your current directory containing cartpole.scs. You can choose to download all of our examples from our Gitlab repository via this zip archive. Extract the contents of the archive into a folder called examples and unzip cartpole.scs.zip. Alternatively, you can run the following commands:

```
$ mkdir -p examples && cd examples
$ wget https://gitlab.lrz.de/i7/dtcontrol/-/raw/master/examples/cartpole.scs.zip
$ unzip cartpole.scs.zip
```

Next, activate the virtual environment you installed dtControl in:

```
$ source dtcontrol-venv/bin/activate
```

Running your first command

Finally, you can run dtControl with the default parameters on the *cartpole* example (cartpole.scs), use the following command:

(dtcontrol-venv) \$ dtcontrol --input examples/cartpole.scs

This will produce some new files and folders in the current folder:

```
decision_trees
|-- default
| `-- cartpole
| |-- default.c
| |-- default.dot
benchmark.json
benchmark.html
```

Open benchmark.html in your favourite browser to view a summary of the results. For more details on what these files are, see *Understanding the output*.

Presets and configuration files

dtControl allows the user to configure the learning algorithm using "presets" defined in a "configuration file". The presets can be chosen using the --use-preset switch and the configuration file can be chosen using the --config switch. For your convenience, we have pre-defined a bunch of preset configurations that we believe are interesting. You can list the available presets by running:

(dtcontrol-venv) \$ dtcontrol preset --list

This should produce the following table of presets.

name	numeric-predicates	categorical-	deter-	impu-	toler-	safe-
		predicates	minize	rity	ance	pruning
default	['axisonly']	['multisplit']	none	en-	1e-05	False
				tropy		
cart	['axisonly']		none	en-		
				tropy		
linsvm	['axisonly', 'linear-		none	en-		
	linsvm']			tropy		
logreg	['axisonly', 'linear-		none	en-		
	logreg']			tropy		
oc1	['oc1']		none	en-		
				tropy		
maxfreq	['axisonly']		maxfreq	en-		
				tropy		
maxfreqlc	['axisonly', 'linear-		maxfreq	en-		
	logreg']			tropy		
minnorm	['axisonly']		minnorm	en-		
				tropy		
minnormlc	['axisonly', 'linear-		minnorm	en-		
	logreg']			tropy		
SOS	['axisonly']		none	en-		
				tropy		
SOS-	['axisonly']		none	en-		True
safepruning				tropy		
linear-auroc	['axisonly', 'linear-		none	auroc		
	logreg']					

The --use-preset argument takes in one or more preset names as argument. For each preset specified as argument, dtControl will run the learning algorithm configured as described in this table and produce results in the folder: decision_trees/et_name</createdocument/</pre>

Configurable options

- 1. **numeric-predicates** can be used to configure the class of predicates that are considered for constructing the tree. It can take the values
 - a. axisonly for predicates which compare a variable to a constant
 - b. linear-logreg for predicates which compare a linear combination of variables to a constant (ax + by < c) obtained using Logistic Regression</p>
 - c. linear-linsvm for linear predicates obtained using linear Support Vector Machines, and finally
 - d. ocl for predicates obtained from the tool of Murthy et. al
- 2. categorical-predicates determines how non-numeric or categorical variables (such as color = blue) should be dealt with. Currently, it only supports the option
 - a. multisplit which creates a decision node with as many children as the number of possible categories the variable can take (e.g. color = blue, color = green and color = red).
 - b. singlesplit which creates a decision node with just two children, one satisfying a categorical equality (color = blue) and the other that does not (color != blue).
 - c. valuegrouping as described in M. Jackermeier's thesis (TODO link)

- 3. **determinize** determines the type of determinization used on permissive/non-deterministic controller when constructing the tree. Possible options are
 - a. none to preserve permissiveness,
 - b. minnorm to pick control inputs with the minimal norm,
 - c. maxnorm to pick control inputs with the maximal norm,
 - d. random to pick a control input uniformly at random,
 - e. maxfreq to pick our in-house developed determinization strategy, details of which are available in M. Jackermeier's thesis (TODO link).
 - f. auto to let dtControl automatically choose a determinization strategy; currently defaults to maxfreq.
- 4. **impurity** allows users to choose the measure by which splitting predicates are evaluated. Possible options are
 - a. entropy
 - b. gini
 - c. auroc
 - d. maxminority
 - e. twoing
 - f. multilabelentropy
 - g. multilabelgini
 - h. multilabeltwoing
- 5. tolerance is a floating point value relevant only when choosing the valuegrouping categorical predicate.
- 6. safe-pruning decides whether to post-process the decision tree as specified in Ashok et. al. (2019).

Creating your own presets

As a user, you can define your own preset by mixing and matching the parameters from *Configurable options*. The presets must be defined inside a .yml file as follows:

```
presets:
  my-config:
    determinize: maxfreq
    numeric-predicates: ['axisonly']
    categorical-predicates: ['singlesplit']
    impurity: 'entropy'
    safe-pruning: False
    another-config:
    determinize: minnorm
    numeric-predicates: ['linear-logreg']
    categorical-predicates: ['valuegrouping']
    tolerance: 10e-4
    safe-pruning: False
```

Note: The values for the keys numeric-predicates and categorical-predicates are lists. If the list contain more than one elements, e.g. numeric-predicates: ['axisonly', 'linear-svm'], dtControl will construct predicates for each of the classes present (in this case, both axis-parallel and linear splits using a linear SVM) in the list and pick the best predicate amongst all the classes.

The above sample presets can be generated automatically and wrote into a user-config.yml file by running:

(dtcontrol-venv) \$ dtcontrol preset --sample > user-config.yml

Now, dtControl can be run on the *cartpole* example with the my-config preset by running:

```
(dtcontrol-venv) $ dtcontrol --input examples/cartpole.scs --config user-config.yml --

→use-preset my-config
```

Understanding the output

Once dtControl is used to run some experiments, you may notice a bunch of new files and folders:

```
decision_trees
|-- default
   `-- cartpole
|-- default.c
|-- default.dot
|-- my-config
  `-- cartpole
|-- my-config.c
|-- my-config.dot
benchmark.json
benchmark.html
```

- benchmark.html is the central file, which summarizes all the results obtained by dtControl. It may be opened using a browser of your choice.
- benchmark.json is a JSON file containing all the statistics collected by the tool (tree size, bandwidth, construction time and other metadata). The benchmark.html file is rendered from this JSON file at the end of the experiments.
- default.c contains the C-code of the decision tree
- default.dot contains the DOT source code which can be compiled using the dot -Tpdf default. dot -o default.pdf command or viewed using a web-based tool

By default, the decision trees are stored in the decision_trees folder and the statistics are stored in the benchmark.json and benchmark.html files. This can however be customized with the help of the --output and the --benchmark-file switches. For example:

Will produce the following files and directories:

```
cartpole_trees
|-- my-config
| `-- cartpole
| |-- my-config.c
| |-- my-config.dot
cartpole_stats.json
cartpole_stats.html
```

Timeout

Another useful feature is timeout which can be set with the --timeout/-t switch. For example,:

\$ dtcontrol --input examples/truck_trailer.scs --timeout 3m

will run CART on the *truck_trailer* example, and time out if it is taking longer than 3 minutes to finish. The --timeout/-t switch can accept timeout in seconds, minutes and hours (-t 42s or -t 30m or -t 1h). The timeouts is applied for each preset individually, and not for the whole set of experiments.

Re-run

By default, new results are appended to benchmark.json (or the file passed to the --benchmark-file switch) and experiments are not re-run if results already exist. In case you want to re-run a method and overwrite existing results, use the --rerun flag.:

\$ dtcontrol --input examples/cartpole.scs --rerun

1.1.3 Quick Start with the Python Interface

More advanced users can use dtControl programmatically using Python or as part of a Jupyter notebook. Here is an example of the Python interface with comments that give guidance on what is happening:

```
# imports
# you might have to import additional classifiers
from sklearn.linear model import LogisticRegression
from dtcontrol.benchmark_suite import BenchmarkSuite
from dtcontrol.decision tree.decision tree import DecisionTree
from dtcontrol.decision tree.determinization.max freq determinizer import
→ MaxFreqDeterminizer
from dtcontrol.decision_tree.impurity.entropy import Entropy
from dtcontrol.decision tree.impurity.multi label entropy import MultiLabelEntropy
from dtcontrol.decision_tree.splitting.axis_aligned import.
→AxisAlignedSplittingStrategy
from dtcontrol.decision tree.splitting.linear classifier import
→LinearClassifierSplittingStrategy
# instantiate the benchmark suite with a timeout of 2 hours
# rest of the parameters behave like in CLI
suite = BenchmarkSuite(timeout=60*60*2,
                       save folder='saved classifiers',
                       benchmark_file='benchmark',
                       rerun=False)
# Add the 'examples' directory as the base where
# the different controllers will be searched for
# You can also choose to only include specific files
# in the directory with the 'include' and 'exclude' list
suite.add_datasets('examples')
# setting up the predicates
aa = AxisAlignedSplittingStrategy()
logreg = LinearClassifierSplittingStrategy(LogisticRegression, solver='lbfgs',...

→penalty='none')
```

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```
# select the DT learning algorithms we want to run and give them names
classifiers = [
    DecisionTree([aa], Entropy(), 'CART'),
    DecisionTree([aa], Learly], Entropy(), 'LogReg'),
    DecisionTree([aa], Entropy(), 'Early-stopping', early_stopping=True),
    DecisionTree([aa], Entropy(MaxFreqDeterminizer()), 'MaxFreq', early_
    istopping=True),
    DecisionTree([aa], MultiLabelEntropy(), 'MultiLabelEntropy', early_stopping=True)
]
# finally, execute the benchmark
suite.benchmark(classifiers)
# open the web browser and show the result
suite.display_html()
```

As you can see, the Python interface provides mostly the same parameters as the CLI, but gives you some additional control. In particular, the following functionality is currently only supported by the Python interface:

- Using early_stopping with the label powerset method
- · Parameters for safe pruning and early stopping which control the amount of nondeterminism preserved
- Choosing any determinizer for oblique splits
- · Only allowing oblique splits in leaf nodes
- Various parameters of the OC1 heuristic
- The ScaledBincount impurity measure with a custom scaling function

The easiest way to get more information on the methods available in the Python interface is to directly browse the source code of dtControl.

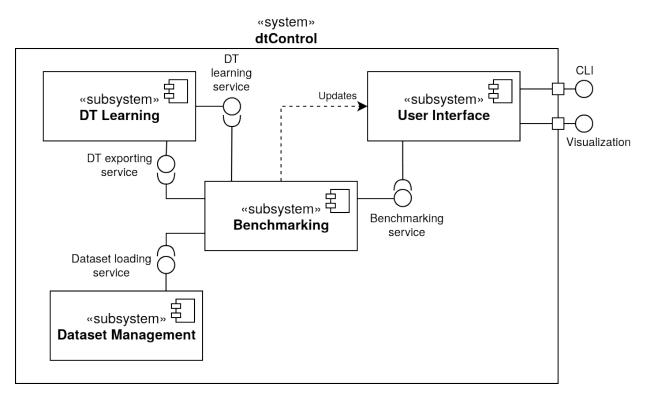
1.2 Developer Manual

This document aims to provide the reader with the necessary information to be able to extend or customize dtControl. We first give an overview of the general software architecture of the tool. Then, we show how support for controllers in new file formats can be added, explain the inner workings of the decision tree (DT) learning component, and explore how dtControl could be extended with new output formats.

1.2.1 Overview

dtControl is written entirely in Python and makes use of both the numpy and scikit-learn packages for data representation and manipulation. A basic familiarity with this programming environment is assumed throughout this manual. More information on dependencies can be found in the provided readme and setup.py files.

An overview of the software architecture of dtControl is given in the following UML component diagram:



The heart of the tool is formed by the *DT Learning* subsystem, which is responsible for the actual decision tree algorithms and representation. It provides all of the different options for training DTs and can export the learned trees in the DOT and C format.

To make the DT learning itself independent of any verification tool, the *Dataset Management* has been extracted into a separate subsystem, which mainly provides functionality for loading and converting controllers from many different sources such as SCOTS, Uppaal Stratego, and PRISM.

The *Benchmarking* component is responsible for running a set of different given DT learning configurations on a number of specified controllers. It thus uses both the functionality provided by the Dataset Management and the DT Learning subsystems.

Finally, the *User Interface* serves as the main entry point for user interaction with the tool, in the form of a CLI. The constructed HTML files with benchmark statistics also belong to the user interface.

1.2.2 Supporting new file formats

dtControl currently supports the file formats generated by the the tools SCOTS, Uppaal Stratego, and PRISM. There are two ways to make the tool work with other formats, as described in the following.

The CSV format

The first option is to convert the new file format to a custom CSV format that dtControl also supports. We now describe the specification of the custom CSV format.

The first two lines of the file are reserved for metadata. The first line must always reflect whether the controller is permissive (non-deterministic) or non-permissive (deterministic). This is done using either of the following lines:

#PERMISSIVE

or:

#NON-PERMISSIVE

The second line must reflect the number of state variables (or the state dimension) and the number of control input variables (or the input dimension). This line looks as follows:

#BEGIN N M

where N is the state dimension and M is the input dimension.

Every line after the 2nd line lists the state action/input pairs as a comma separated list:

x1,x2,...,xN,y1,y2,...,yM

if the controller prescribes the action (y1, y2, ..., yM) for the state (x1, x2, ..., xN). If the state allows more actions, for example, (y1', y2', ..., yM'), then this should be described on a new line:

```
x1, x2, ..., xN, y1, y2, ..., yM
x1, x2, ..., xN, y1', y2', ..., yM'
```

An excerpt of the 10rooms.scs controller written in this CSV format would look as follows:

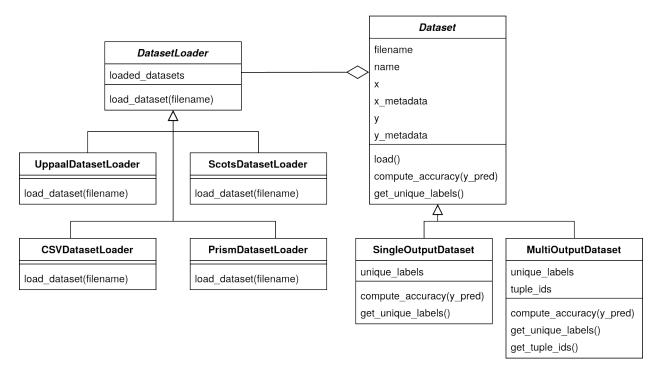
```
#PERMISSIVE
#BEGIN 10 2
18.75,20.0,18.75,18.75,20.0,18.75,18.75,18.75,18.75,18.75,18.75,1.0,1.0
20.0,20.0,18.75,18.75,20.0,18.75,18.75,18.75,18.75,18.75,1.0,1.0
21.25,20.0,18.75,18.75,20.0,18.75,18.75,18.75,18.75,18.75,18.75,1.0,1.0
18.75,21.25,18.75,18.75,20.0,18.75,18.75,18.75,18.75,18.75,18.75,0.0,1.0
18.75,21.25,18.75,18.75,20.0,18.75,18.75,18.75,18.75,18.75,1.0,1.0
20.0,21.25,18.75,18.75,20.0,18.75,18.75,18.75,18.75,18.75,18.75,0.0,1.0
```

dtControl will automatically look for files with a .csv extension and parse them with the assumption that they follow this format.

Implementing a new dataset loader - the dataset management subsystem

Additionally, it is also possible to integrate the new file format natively into dtControl by providing a dataset loader. For this, we will take a closer look at the *Dataset Management* subsystem.

An overview of the subsystem is given in the following UML class diagram:



The Dataset class is what the DT learning algorithm needs to train a decision tree. A Dataset can either be a SingleOutputDataset if it only has a single control input, or a MultiOutputDataset if there are multiple control inputs.

Note: Since the code focuses on the decision trees themselves, it refers to the *output* of those trees, which is the same as the action produced by the controller, i.e. the control *input*.

Its most important properties are detailed in the following:

- x is a simple NumPy array containing the values of the state variables. It has dimension #number of states in the controller #number of state variables.
- x_metadata is a dictionary containing metadata about the array x. For instance, it contains the names of the variables (if available), the minimum and maximum value in x, and indicates which columns of x are categorical.
- y is a NumPy array containing the actions that can be performed for every state. Its format differs, depending on whether the dataset is single- or multi-output:
 - In the case of single-output datasets, y is a two-dimensional array where each row contains all (non-deterministic) actions that can be performed at the corresponding row of x. Instead of the actual (possibly) floating point values, we use integer indices representing those values throughout the code; the mapping of indices to the actual values can be found in dataset.index_to_value. Since NumPy usually cannot deal with rows of different sizes, but we have varying numbers of possible actions, some rows have to be filled with -1 s. These -1 s have to be ignored during tree construction.
 - In the case of multi-output datasets, y is a three-dimensional array whose first dimension (or axis) corresponds to the different control inputs. Thus, there is a two-dimensional array for each control-input, which exactly matches the structure outlined above. The DT learning algorithms implemented so far all convert from this representation to the *tuple ID* representation in which every action (y1, y2, ..., yM) is replaced with a single tuple id. The method get_tuple_ids() returns an array of labels in this tuple ID representation, which again matches the structure of the y array in the single-output case.

• y_metadata is a dictionary containing metadata about the array y. Similarly to x_metadata, it indicates which columns of y are categorical outputs, and provides some other information such as the minimum and maximum value in y.

The Dataset class provides some auxiliary functionality for the DT learning algorithm, such as compute_accuracy(y_pred) and get_unique_labels(), as well as a load() method that uses a DatasetLoader to actually load the dataset from a file into the internal NumPy representation.

It is this DatasetLoader class that needs to be extended in order to add support for a new file format to dtControl. A new DatasetLoader must provide exactly one method: $load_dataset()$ parses a file in the new format and returns the tuple (x, x_metadata, y, y_metadata, index_to_value) which corresponds to the attributes of a Dataset as outlined above.

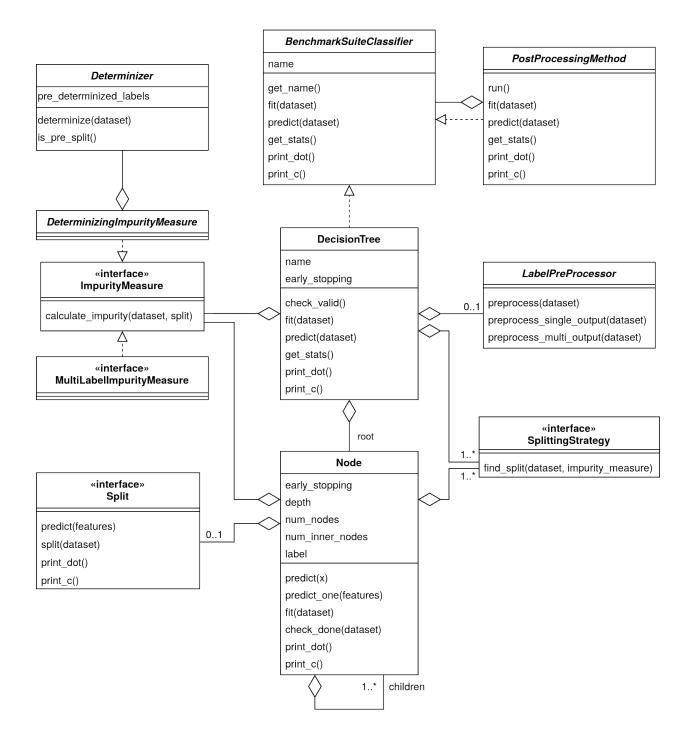
The new dataset loader can be registered in the extension_to_loader dictionary in the Dataset class. Now, if dtControl encounters a file with an extension of the new file format, it will attempt to load it using the registered loader.

You may find inspiration for writing your own dataset loader in some of the already existing ones such as the UppaalDatasetLoader or the relatively simple PrismDatasetLoader. However, they are very specific to their respective file format.

1.2.3 Extending dtControl with new algorithms - the decision tree learning subsystem

dtControl already supports a wide variety of decision tree construction algorithms. Furthermore, the tool can readily be extended with new algorithms, as we will see in this section.

We again start with a UML diagram of the DT learning subsystem. In order to keep it as flexible as possible, we use a composition-based approach that makes heavy use of interfaces. This has the advantage that you only need to develop against a specific interface if you want to only extend a part of the DT learning algorithm. For instance, if you want to add a new impurity measure, you just have to provide an implementation of the ImpurityMeasure interface and your code will immediately integrate with the rest of the learning algorithm.



As can be seen, the heart of the component is the DecisionTree class, which offers the core methods one would expect:

- fit (dataset) constructs a decision tree for a dataset.
- predict (dataset) returns a list of control inputs predicted for a dataset.
- get_stats() returns the statistics to be displayed in the benchmark results as a dictionary. This will mainly include the number of nodes and potentially some algorithm-specific statistics.
- export_dot () saves a representation of the decision tree in the DOT format.

• export_c() exports the decision tree to a C-file as a chain of if-else statements.

Most of these methods simply delegate to the root object of type Node, which implements the actual decision tree data structure. It has mostly the same attributes as a DecisionTree, as well as some statistics and either a list of children or a label. Depending on the dataset and algorithm, a label can be one of the following:

- A single integer (that appears in the index_to_value dictionary) corresponding to a single action
- A single tuple of integers corresponding to a single action with multiple outputs
- A list of integers corresponding to multiple possible actions
- A list of tuples corresponding to multiple possible actions with multiple outputs

We now examine the most important interfaces in detail.

Splitting strategies

A SplittingStrategy provides the method find_split(dataset, impurity_measure), which returns the best predicate of a certain type, given a dataset and an impurity measure. For instance, the AxisAlignedSplittingStrategy searches through all possible axis-aligned splits for the given dataset and returns the one with lowest impurity.

The returned predicate is of type Split and must provide the following methods:

- predict (features) returns an index into the children list of a Node corresponding to the child that should be picked for the given NumPy array of features.
- get_masks(dataset) returns a list of NumPy masks indicating how the dataset is split. A mask is just a one-dimensional array of boolean values with a length of len(dataset). A value of True in the jth row of the ith mask indicates that the jth row in dataset.x belongs to the ith sub-dataset created by the split.
- print_dot () returns the string that should be put in the node in the DOT format.
- print_c() returns the string that should be put in the corresponding if-statement in the C code.

The simplest example of a Split is probably the AxisAlignedSplit.

Impurity measures

An ImpurityMeasure needs to provide the calculate_impurity(dataset, split) method, which simply returns a float indicating the impurity. There are two types of impurity measures:

- MultiLabelImpurityMeasures directly compute the impurity from the nondeterministic labels. Examples include MultiLabelEntropy and MultiLabelGiniIndex.
- DeterminizingImpurityMeasures correspond mostly to the traditional impurity measures known from decision trees in machine learning. Examples include Entropy and GiniIndex. These impurity measures are called *determinizing* since they don't directly work on the nondeterministic labels. Instead, the use a Determinizer that first converts the labels to a new representation.

By default, the LabelPowersetDeterminizer is used, which treats every combination of possible labels as a unique label and thus preserves all of the nondeterminism present in the original controller. Other options are for example the MaxFreqDeterminizer, which implements the maximum frequency determinization technique. Determinizers can either be applied before or after splitting, as indicated by the is_pre_split() method.

Determinization

The final ingredient of the DT learning algorithm - determinization - is mainly controlled by the <code>early_stopping</code> attribute of a <code>DecisionTree</code>. If it is set to <code>True</code>, early stopping is performed and the resulting DT is thus (possibly) smaller and more deterministic. This parameter should always be enabled if impurity measures that make use of determinization are used, such as the <code>MultiLabelEntropy</code> or any <code>DeterminizingImpurityMeasure</code> with the <code>MaxFreqDeterminizer</code>.

Instead, one can also choose to determinize the controller itself before DT learning with a LabelPreProcessor, such as the NormPreProcessor. For this, the methods preprocess_single_output(dataset) and preprocess_multi_output(dataset) that return a NumPy array of determinized labels must be provided.

Finally, decision trees can also be post-processed by a PostProcessingMethod such as safe pruning. The most important method of the class is run (), which runs the post-processing technique on its classifier, transforming the decision tree.

1.2.4 Supporting new output formats

As shown above, the core decision tree data structure is implemented in the DecisionTree and Node classes. These classes also offer functionality for DOT and C printing.

To add a new output format to dtControl, one thus would have to provide new exporting methods in the DecisionTree and Node classes. Furthermore, the BenchmarkSuite would have to be adapted to export the tree to the new output format once a DT has been constructed.